Yeast with a diameter of  $5.0 \mu m$  and density of 1.03 g/mL are in a 1.00 g/mL solution having a viscosity of 1.8 cP. What is the settling velocity of these particles?

A flocculent has been added which increases the mean particle diameter to  $100 \mu m$ . What is the settling velocity of these particles?

## E.2

A laboratory centrifuge is used to collect yeast cells after fermentation. During centrifugation the distance between the liquid surface and the axis of rotation is 3 cm. The distance from the top of the liquid surface to the bottom of the centrifuge tubes is 7 cm. The yeast cells are 5  $\mu$ m in diameter and have a density of 1.03 g/mL. The fluid has viscosity of 1 cP and density of 1.00 g/mL.

- a) If the centrifuge is operated at 1,000 rpm, how long is required to pelletize the yeast completely?
- b) If the centrifuge is operated at 5,000 rpm, how long is required to pelletize the yeast completely?
- c) If the tube is sitting upright on the benchtop, how long is required to pelletize the yeast completely?

## E.3

Animal cells are cultivated on dextran bead microcarriers having a density of 1.02~g/mL and a diameter of  $150~\mu m$ . A 50 liter operating volume tank having a diameter of 30~cm is used to cultivate cells grown on microcarriers to produce a vaccine. After growth, the stirring is stopped and the microcarriers are allowed to settle. The microcarrier-free fluid is then withdrawn to isolate the vaccine. The fluid has a density of 1.00~g/mL and a viscosity of 1.1~cP. Find:

- a) The settling velocity of the microcarriers.
- b) The Reynolds Number of the microcarriers.
- c) The time needed for the microcarriers to settle completely.

Unfortunately, yeast cells and *Lactoccocus lactis* have densities that are very close (about  $1.03~\rm g/cm^3$ ), and it is impractical to separate the two types of cells using equilibrium sedimentation. However, the cells are much different in size, with the particular yeast cell being 8  $\mu$ m in diameter, and the bacterial cell being 1.0  $\mu$ m in diameter. This difference in size has led you to consider a way to remove, at least partially, the bacterial cells from the yeast cells.

You start with a 20 mL tube that is 16 cm in height containing  $10^8$  yeast and  $10^7$  bacteria. The medium has a viscosity of 1.2 cP and a density of 1.00 g/cm<sup>3</sup>.

Your idea is the centrifuge until all the yeast cells are below a certain height in the tube. At this point, some bacteria will remain in the upper portion of the tube. You remove the upper bacteria-containing portion carefully, then add fresh buffer to 20 mL and resuspend all the cells. You repeat this process. Then you repeat this process a third time. The fourth time you centrifuge the cells, you just discard the bacteria containing upper portion, leaving yeast cells with fewer bacterial cells.

- a) How many bacterial cells remain if each time you centrifuge enough so that all the yeast are below the 8 cm line of the tube (half-way)?
- b) How many bacterial cells remain if each time you centrifuge enough so that all the yeast are below the 4 cm line of the tube (three-quarters of the fluid is yeast-free)?
- c) If you select the process described in b) above, what g-force will you need for each centrifugation step to take 20 minutes?